

## ***CORRIGE DU SUJET 1***

### **CORRIGE DE L'EXERCICE 1**

On subdivise la section en trois rectangles de  $120 \text{ mm} \times 20 \text{ mm}$  et un autre de  $240 \text{ mm} \times 20 \text{ mm}$ .

- Le centre de gravité de la section:

$$Y_G = \frac{\sum y_i S_i}{\sum S_i} = \frac{2 \times 50 \times 2400}{3 \times 120 \times 20 + 240 \times 20} = 20 \text{ mm}$$

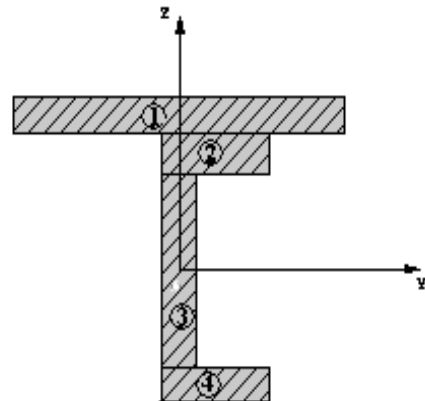
$$Z_G = \frac{\sum z_i S_i}{\sum S_i} = \frac{90 \times 240 \times 20}{3 \times 120 \times 20 + 240 \times 20} = 36 \text{ mm}$$

- Les moments d'inertie centraux:

$$I_y = \sum I_{yi} + \sum S_i a_i^2$$

$$I_z = \sum I_{zi} + \sum S_i b_i^2$$

$$I_{yz} = \sum I_{yzi} + \sum S_i a_i b_i$$



$$I_y = \frac{20 \times 120^3}{12} + 2 \times \frac{120 \times 20^3}{12} + \frac{240 \times 20^3}{12} + 2400 \times 36^2 + 2400 \times 34^2 + 2400 \times 106^2 + 4800 \times 54^2 = 50.05 \times 10^6 \text{ mm}^4$$

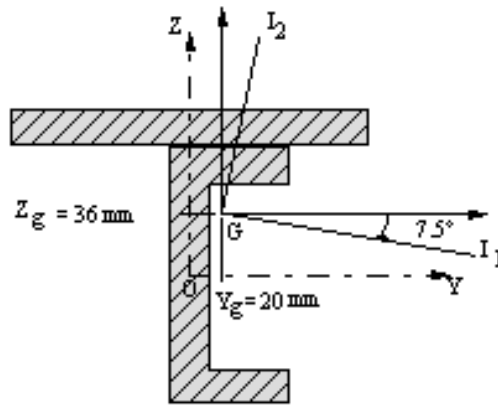
$$I_z = \frac{120 \times 20^3}{12} + 2 \times \frac{20 \times 120^3}{12} + \frac{20 \times 240^3}{12} + 2400 \times 20^2 + 2 \times 2400 \times 30^2 + 4800 \times 20^2 = 36.08 \times 10^6 \text{ mm}^4$$

$$I_{yz} = 2400 \times 30 \times (-106) + 2400 \times 20 \times 36 + 2400 \times 30 \times 36 + 4800 \times 20 \times 54 = 1.87 \times 10^6 \text{ mm}^4$$

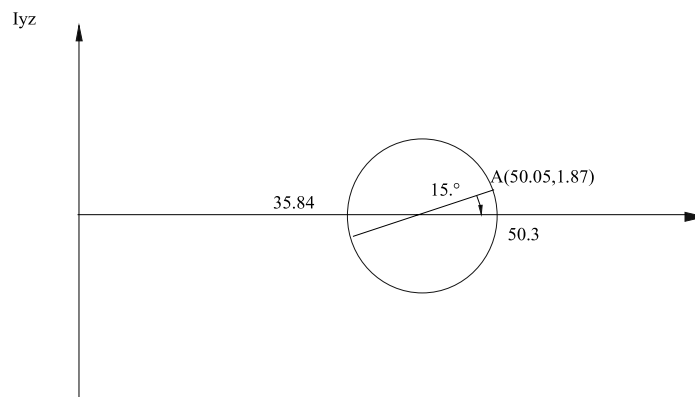
Les moments d'inertie principaux et centraux et leur orientation :

$$\text{tg} 2\alpha_0 = \frac{2 \times 1.87}{36.08 - 50.05} \Rightarrow \alpha_0 = -7.5^\circ$$

$$I_{1,2} = \frac{50.05 + 36.08}{2} \pm \sqrt{\left(\frac{50.05 - 36.08}{2}\right)^2 + 1.87^2} \Rightarrow \begin{aligned} I_1 &= 50.30 \times 10^6 \text{ mm}^4 \\ I_2 &= 35.84 \times 10^6 \text{ mm}^4 \end{aligned}$$



On trace le cercle de Mohr:



## CORRIGE DE L'EXERCICE 2

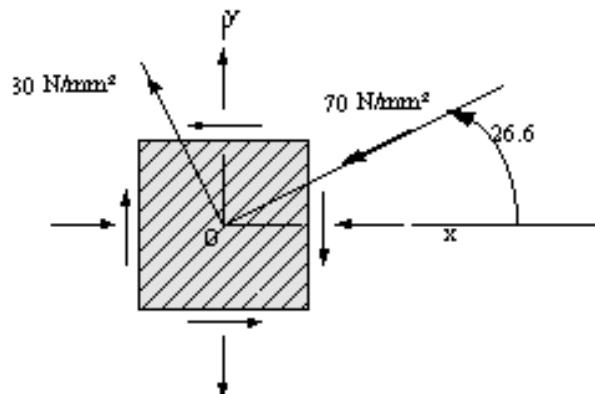
L'orientation de contraintes principales:

$$\operatorname{tg} 2\theta_0 = \frac{2 \times (-40)}{-50 - 10} = 1.33 \Rightarrow \theta_0 = 26.57^\circ$$

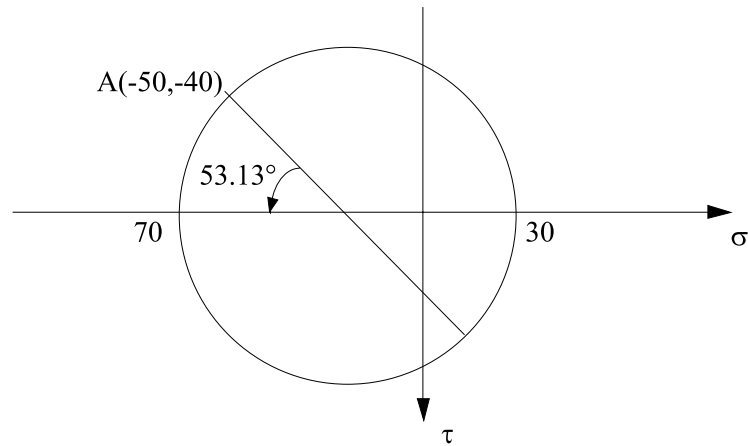
Les contraintes principales:

$$\sigma_{1,2} = \frac{-50 + 10}{2} \pm \sqrt{\left(\frac{-50 - 10}{2}\right)^2 + 40^2} \Rightarrow \begin{aligned} \sigma_1 &= 30 \text{ N/mm}^2 \\ \sigma_2 &= -70 \text{ N/mm}^2 \end{aligned}$$

Orientation des axes principaux sur la facette initiale:



Tracé du cercle de Mohr:



**CORRIGE DE L'EXERCICE 3**

Calcul des réactions:

$$\sum F \uparrow = 0 \Rightarrow V_A + V_B = 60 \tag{1}$$

$$\sum F \rightarrow = 0 \Rightarrow H_A - H_B = 0 \tag{2}$$

$$\sum M_{/A} = 0 \Rightarrow V_B(10\sqrt{2} + 5\sqrt{5}) + 5H_B = 60(10\sqrt{2} + 2) \tag{3}$$

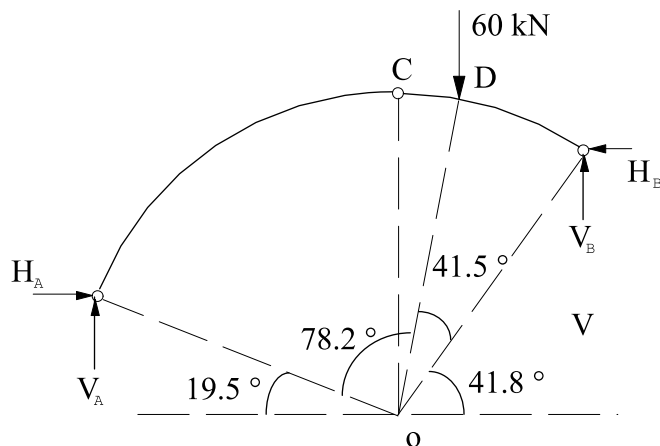
$$\sum M_{/Cd} = 0 \Rightarrow V_B(5\sqrt{2}) - 5H_B = 60 \times 2 \tag{4}$$

de (3) et (4)

$$V_B = 29.8\text{kN} \text{ et } H_B = 42.7\text{kN}$$

et de (1) et (2) on obtient:

$$V_A = 30.2\text{kN} \text{ et } H_A = 42.7\text{kN}$$



**Diagramme des efforts internes:****Tronçon AD  $0 \leq \theta \leq 78.2$** 

$$N = -30.2 \cos(19.47 + \theta) - 42.7 \sin(19.47 + \theta)$$

$$N(0) = -42.72 \text{ kN}, N(70.5) = -42.7 \text{ kN}, N(78.2) = -38.3$$

$$T = 30.2 \sin(19.47 + \theta) - 42.7 \cos(19.47 + \theta)$$

$$T(0) = -30.17 \text{ kN}, T(70.5) = 30.2 \text{ kN}, T(78.2) = 35.62, T(\theta) = 0 \Rightarrow \theta = 35.3$$

$$M = 30.2 \times 15 [\cos 19.47 - \cos(19.47 + \theta)] - 42.7 \times 15 [\sin(19.47 + \theta) - \sin 19.47]$$

$$M(0) = 0, M(70.5) = 0, M(78.2) = 66.18, M_{\max} = M(35.3) = -143.7$$

**Tronçon BD  $0 \leq \theta \leq 40.54$** 

$$N = -29.8 \cos(41.8 + \theta) - 42.7 \sin(41.8 + \theta)$$

$$N(0) = -50.68 \text{ kN}, N(40.54) = -46.3 \text{ kN}$$

$$T = -29.8 \sin(41.8 + \theta) + 42.7 \cos(41.8 + \theta)$$

$$T(0) = 11.97 \text{ kN}, T(40.54) = -23.84 \text{ kN}, T(\theta) = 0 \Rightarrow \theta = 13.3$$

$$M = 29.8 \times 15 [\cos 41.8 - \cos(41.8 + \theta)] - 42.7 \times 15 [\sin(41.8 + \theta) - \sin 41.8]$$

$$M(0) = 0, M(40.54) = 65.81, M_{\max} = M(13.3) = -20.91$$

